

ON THE COFINITENESS OF GENERALIZED LOCAL COHOMOLOGY MODULES

(SCIE)

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TÓM TẮT:

Let R be a commutative Noetherian ring, I an ideal of R and M, N two finitely generated R -modules. The aim of this paper is to investigate the I -cofiniteness of generalized local cohomology modules $H^j_I(M;N)$ of M and N with respect to I . We first prove that if I is a principal ideal then $H^j_I(M;N)$ is I -cofinite for all $M;N$ and all j . Secondly, let t be a non-negative integer such that $\dim \text{Supp}(H^j_I(M;N)) \leq 1$ for all $j < t$. Then $H^j_I(M;N)$ is I -cofinite for all $j < t$ and $\text{Hom}(R/I; H^t_I(M;N))$ is finitely generated. Finally, we show that if $\dim(M) \leq 2$ or $\dim(N) \leq 2$ then $H^j_I(M;N)$ is I -cofinite for all j .